How big is infinity?

How many whole numbers are there? What about even whole numbers? Real numbers? We might answer “infinitely many” for all three, and while we’d be correct, there’s more to the story. In other words, the answer to the title question is complicated! We’ll talk about some of the subtle ways in which our intuition might lead us astray when discussing the concept of infinity.