Math 2233 Homework Set 8

1. Determine the lower bound for the radius of convergence of series solutions about each given point x_o .

- (a) y'' + 4y' + 6xy = 0, $x_0 = 0$ (b) (x - 1)y'' + xy' + 6xy = 0, $x_0 = 4$
- (b) $(x 1)y + xy + 6xy = 0, x_0 = 4$ (c) $(4 + x^2)y'' + 4xy' + y = 0, x_0 = 0$
- (d) $(1+x^2)y'' + 4xy' + y = 0, x_0 = 2$

2. Determine the singular points of the following differential equations and state whether they are regular or irregular singular points.

(a) xy'' + (1-x)y' + xy = 0(b) $x^2(1-x)^2y'' + 2xy + 4y = 0$ (c) $(1-x^2)^2y'' + x(1-x)y' + (1+x)y = 0$

3. The following differential equation has a regular singular point at x = 0. Determine the indicial equations, the roots of the indicial equations, the recursion relations, and the first four terms of two linearly independent series solutions.

$$2xy'' + y' + xy = 0$$

4. The following differential equation has a regular singular point at x = 0. Determine the indicial equation and the recursion relations corresponding to the largest root of the indicial equation. Write down the first four terms of the corresponding solution.

(a)
$$xy'' + y = 0$$

(b) $xy'' + (1 - x)y' - y = 0$